

Math 114 Fall 2017  
Calculus I HW 3  
Due Wednesday, September 20

1. Let

$$f(x) = \begin{cases} 1 & x < 2 \\ 2 & x = 2 \\ 3 & x > 2 \end{cases}$$

What is  $f(2)$ ? Prove that  $\lim_{x \rightarrow 2} f(x)$  does not exist.

2. Let

$$j(x) = \begin{cases} 3x - 1 & x < 0 \\ 2x + 1 & x \geq 0 \end{cases}$$

Show that  $\lim_{x \rightarrow 3} j(x) = 7$ .

3. (★) For the same function  $j$ , show that  $\lim_{x \rightarrow 0} j(x)$  does not exist.
4. (★) Prove that  $\lim_{x \rightarrow 0} \frac{|x|}{x}$  does not exist.
5. Compute from the definition  $\lim_{x \rightarrow 2} \frac{1}{x-2}$ .
6. Compute from the definition  $\lim_{x \rightarrow 5} \frac{x-2}{x-5}$ .
7. Compute from the definition  $\lim_{x \rightarrow -3} \frac{-1}{(x+3)^4}$ .