

Math 1232 Spring 2022  
Single-Variable Calculus 2 Mastery Quiz 6  
Due Tuesday, February 22

This week's mastery quiz has four topics. Everyone should submit S4 and S5. If you have a 4/4 on M2, meaning you got 2/2 on each of your first two attempts, you shouldn't submit that. If you have a 2/2 on S3 from last week, you shouldn't submit that.

Feel free to consult your notes or speak to me privately, but please don't talk about the actual quiz questions with other students in the course or post about it publicly.

Don't worry if you make a minor error, but try to demonstrate that you understand the concepts involved and have mastered the underlying material. For all these problems, justify your answers and explain how you reached them. Do not just write "yes" or "no" or give a single number.

Please turn this quiz in class on Tuesday. You may print this document out and write on it, or you may submit your work on separate paper; in either case make sure your name and recitation section are clearly on it. If you absolutely cannot turn it in in person, you can submit it electronically through Blackboard but this should be a last resort.

**Topics on This Quiz**

- Major Topic 2: Advanced Integration Techniques
- Secondary Topic 3: Numeric Integration
- Secondary Topic 4: Improper Integrals
- Secondary Topic 5: Arc Length and Surface Area

**Name:**

**Recitation Section:**

**M2: Advanced Integration Techniques**

(a)  $\int_{\pi/9}^{\pi/6} x \cos(3x) dx =$

(b)  $\int_0^{\pi/6} \sec^3(2t) \tan(2t) dt =$

(c) Compute  $\int \frac{x^2+x+3}{x-2} dx =$

### S3: Numeric Integration

- (a) How many intervals do you need with the **trapezoid** rule to approximate  $\int_5^9 (x+4)^{3/2} dx$  to within  $1/10$ ? Compute that approximation. (Feel free to use a calculator to plug in numeric values, or to leave the answer in exact unsimplified terms, but show every step.)

- (b) Suppose we have

$$g(0) = 5 \quad g(1) = 4 \quad g(2) = 7 \quad g(3) = 4 \quad g(4) = 2 \quad g(5) = 3 \quad g(6) = 5$$

Approximate  $\int_0^6 g(x) dx$  using the Midpoint rule and using Simpson's rule.

**S4: Improper Integrals**

(a) Compute  $\int_1^{\infty} \frac{\ln(x)}{x^2} dx =$

(b) Compute  $\int_1^3 \frac{x}{x^2 - 1} dx =$

**S5: Arc Length and Surface Area**

(a) Compute the arc length of the curve  $(y - 2)^3 = x^2$  between  $y = 2$  and  $y = 6$ .

(b) Set up (but don't compute!) an integral for the area of a surface obtained by taking the curve  $y = \ln(x^3 + 1)$  from  $x = 0$  to  $x = 10$  and rotating around the  $x$  axis.