

Math 1232 Spring 2023  
Single-Variable Calculus 2 Section 12  
Mastery Quiz 10  
Due Tuesday, April 11

This week's mastery quiz has three topics. You should definitely submit all three of them. Don't worry if you make a minor error, but try to demonstrate your mastery of the underlying material. Feel free to consult your notes, but please don't discuss the actual quiz questions with other students in the course.

Remember that you are trying to demonstrate that you understand the concepts involved. For all these problems, justify your answers and explain how you reached them. Do not just write "yes" or "no" or give a single number.

Please turn this quiz in class on Tuesday. You may print this document out and write on it, or you may submit your work on separate paper; in either case make sure your name and recitation section are clearly on it. If you absolutely cannot turn it in in person, you can submit it electronically but this should be a last resort.

**Topics on This Quiz**

- Major Topic 3: Series Convergence
- Major Topic 4: Power and Taylor Series as functions
- Secondary Topic 8: Power Series

**Name:**

**Recitation Section:**

### M3: Series Convergence

Analyze the convergence of the following three series. (Specify if they converge absolutely, converge conditionally, or diverge.)

(a)  $\sum_{n=2}^{\infty} \frac{\ln(n) + n}{n^2 - 1}$

(b)  $\sum_{n=1}^{\infty} \frac{n^2 + n - 3}{n^2 4^n}$

(c)  $\sum_{n=1}^{\infty} \frac{(-1)^n \sqrt{n}}{2n + 3}$

### M4: Taylor Series

(a) Write a power series expression for  $\frac{2x^2}{4x+1}$  centered at 0. What is the radius of convergence?

(b) If  $f(x) = \sum_{n=0}^{\infty} \frac{n+1}{n!+1} x^n$ , compute  $\int_3^6 f(x)$ .

(c) Write a power series expression for  $\ln(1+x^2)$  centered at 1. What is the radius of convergence?

### S8: Power Series

(a) Find the radius of convergence and the interval of convergence of  $\sum_{n=1}^{\infty} \frac{(2x-5)^n}{n^2}$ .

(b) Find the radius of convergence and the interval of convergence of  $\sum_{n=1}^{\infty} \frac{n^2 x^n}{1 \cdot 3 \cdot 5 \cdots (2n-1)}$ .