

Math 1232 Spring 2023  
Single-Variable Calculus 2 Section 12  
Optional Mastery Quiz 13  
Due Tuesday, May 2

This week's mastery quiz has three topics. You may not need to submit any of them.

You can submit on Blackboard, or you can hand it in during my office hours on Tuesday. (Or hand it in to the TA directly.)

Don't worry if you make a minor error, but try to demonstrate your mastery of the underlying material. Feel free to consult your notes, but please don't discuss the actual quiz questions with other students in the course.

Remember that you are trying to demonstrate that you understand the concepts involved. For all these problems, justify your answers and explain how you reached them. Do not just write "yes" or "no" or give a single number.

Please turn this quiz in class on Tuesday. You may print this document out and write on it, or you may submit your work on separate paper; in either case make sure your name and recitation section are clearly on it. If you absolutely cannot turn it in in person, you can submit it electronically but this should be a last resort.

**Topics on This Quiz**

- Major Topic 4: Power and Taylor Series as functions
- Secondary Topic 9: Applications of Taylor Series
- Secondary Topic 10: Parametrization

**Name:**

**Recitation Section:**

## M4: Taylor Series

- (a) Using series we already know, write down a formula for the (infinite) Taylor series for  $e^{3x} - e^x$ , and then write down the degree-three polynomial explicitly.

- (b) Let  $f(x) = \sin(x)$ . Use *the definition of a Taylor series* to find  $T_3(x, \pi/3)$  (centered at  $\pi/3$ ) for this function. (That is, find the terms up through the degree-three term.)

Name:

Recitation Section:

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- (c) Write a power series expression for  $\frac{x}{2+x^2}$  centered at 0. What is the radius of convergence?

**S9: Applications of Taylor Series**

(a) Use a Taylor series to compute  $\lim_{x \rightarrow 0} \frac{xe^{x^3} - x - x^4}{x^7} =$

(b) Use a degree-three Taylor polynomial to estimate  $(1.1)^{3.1}$ .

(c) Use a degree-five Taylor polynomial to estimate  $\sin(.3)$ .

(d) Using series, compute  $\int_0^\pi 2x \cos(x^5) dx$ .

**S10: Parametrization**

(a) Find the length of the curve parametrized by  $x = e^t - t, y = 4e^{t/2}$  for  $0 \leq t \leq 2$ .

(b) Find an equation of the line tangent to the curve  $x = \cos^3(t), y = \sin^3(t)$  at the point  $(1/8, -3\sqrt{3}/8)$ .