

Math 1231 Fall 2024  
Single-Variable Calculus I Section 11  
Mastery Quiz 2  
Due Monday, September 9

This week's mastery quiz has two topics. If you have a 2/2 on S1 (as shown on Blackboard), you don't need to submit it again, but if you have a 1/2 or 0/2 you should submit again. Everyone should submit on M1.

Feel free to consult your notes, but please **don't discuss the actual quiz questions with other students in the course**.

Remember that you are trying to demonstrate that you understand the concepts involved. For all these problems, justify your answers and explain how you reached them. Do not just write "yes" or "no" or give a single number.

Please turn this quiz in class on Monday. You may print this document out and write on it, or you may submit your work on separate paper; in either case make sure your name and recitation section are clearly on it. If you absolutely cannot turn it in in person, you can submit it electronically but this should be a last resort.

**Topics on This Quiz**

- Major Topic 1: Computing Limits
- Secondary Topic 1: Estimation

**Name:**

**Recitation Section:**

## Major Topic 1: Computing Limits

(a) Compute  $\lim_{x \rightarrow 3} \frac{\sqrt{x+1} - 2}{x-3} =$

(b) Compute  $\lim_{x \rightarrow 2} \frac{x^2 + x - 5}{3 - x} =$

(c) Compute  $\lim_{x \rightarrow 3} \frac{x^2 - 5x + 6}{x^2 - x - 6} =$

## Secondary Topic 1: Estimation

- (a) Suppose  $f(x) = \sqrt{x-3}$ , and we want an output of approximately 2. What input  $a$  should we aim for? Find a  $\delta$  so that if our input is  $a \pm \delta$  then our output will be  $2 \pm .5$ . Explain how you found this  $\delta$  and why it should give us what we want.

- (b) We want to build a ramp that's eight times long as it is tall, and we want it to reach a height of 10 meters. Find a formula for  $\delta$  in terms of  $\epsilon$ , so that if the error in the *length* is less than  $\delta$  then the error in the height is less than  $\epsilon$ . Make sure your formula gives the **largest  $\delta$  possible**, and justify your answer.