Math 1231 Spring 2024 Single-Variable Calculus I Section 11 Mastery Quiz 10 Due Tuesday, April 2

This week's mastery quiz has three topics. If you have a 4/4 on M3, or a 2/2 on S7 or S8, you don't need to submit them. (Yes, these are all the same topics as last week.)

Feel free to consult your notes, but please don't discuss the actual quiz questions with other students in the course.

Remember that you are trying to demonstrate that you understand the concepts involved. For all these problems, justify your answers and explain how you reached them. Do not just write "yes" or "no" or give a single number.

Please turn this quiz in class on Thursday. You may print this document out and write on it, or you may submit your work on separate paper; in either case make sure your name and recitation section are clearly on it. If you absolutely cannot turn it in person, you can submit it electronically but this should be a last resort.

Topics on This Quiz

- Major Topic 3: Optimization and Extrema
- Secondary Topic 7: Curve Sketching
- Secondary Topic 8: Physical Optimization

Name:

Recitation Section:

Major Topic 3: Optimization and Extrema

- (a) The function $g(x) = x^3 3x^2 9x + 3$ has absolute extrema either on the interval (-2, 4) or on the interval [-2, 4]. Pick one of those intervals, explain why g has extrema on that interval, and find the absolute extrema.
- (b) Classify the critical points and relative extrema of $g(x) = \cos^2(x) 2\sin(x)$ on $[0, 2\pi]$.

Secondary Topic 7: Curve Sketching

Sketch the graph of $f(x) = x^5 - 5x^4 + 5x^3 = x^3(x^2 - 5x + 5)$. We have $f'(x) = 5x^2(x-3)(x-1)$ and $f''(x) = 10x(2x^2 - 6x + 3)$.

You should discuss the domain, limits at infinity, critical points, intervals of increase and decrease, concavity, and possible points of inflection.

Secondary Topic 8: Physical Optimization

We wish to build a rectangular pen with two parallel internal partitions, using 1000 feet of fencing. We want to maximize the total area of the pen.

- (a) What is your objective function, and why?
- (b) What constraint equation(s) can you use?
- (c) What dimensions maximize the total area of the pen?



Name: