Math 1232: Single-Variable Calculus 2 George Washington University Fall 2025 Recitation 2

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Problem 1. (a) Compute $\log_3(6) + \log_3(9/2)$.

- (b) Compute $\log_4(8) \log_4(2)$.
- (c) Rewrite the expression $\log_5(15) + \log_5(75) \log_5(12)$ as an integer plus a logarithm.

(d) Solve
$$e^{5-3s} = 10$$
.

Problem 2. Let $h(x) = \ln |x|$. We're going to compute the derivative of this two ways.

- (a) If we assume x > 0, we can simplify $\ln |x|$. What does it simplify to? What is the derivative?
- (b) If x < 0, we can also simplify $\ln |x|$. What does it simplify to? This is a little less obvious. What is the derivative?
- (c) What about when x = 0?
- (d) What pattern do we get here?
- (e) Now let's approach this a totally different way. Verify that we can define $|x| = \sqrt{x^2}$. How does that work?
- (f) Use the chain rule to compute $\ln(\sqrt{x^2})$. Does this match your previous answer?

Problem 3. Compute the derivative of $(x+1)^{\sqrt{x}}$.

Problem 4. Use logarithmic differentiation to compute $\frac{d}{dx} \frac{x^3 \sqrt{x^2 - 5}}{(x+4)^3}$.

Problem 5. Try to compute the following integrals.

- (a) $\int_0^3 e^x dx$
- (b) $\int_0^{\ln(3)} e^x dx$
- (c) $\int e^{3x} dx$. (Hint: remember *u*-substitution!)
- (d) $\int 3^x dx$. Hint: there are a couple ways you can approach this.